

# Evaluation of generalized depletion modeling of the US *Illex* fishery

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Disclosure: Manderson's contributions to the 2022 *Illex* RT assessment supported by a consortium of processors & independent owner-operators in the US *Illex* fishery

SSC meeting: 05-10-2022

## Review article

Contribution to the Symposium: 'Johan Hjort Symposium 2019'

## Stock assessment and management of cephalopods: advances and challenges for short-lived fishery resources

Alexander I. Arkhipkin <sup>1\*</sup>, Lisa C. Hendrickson <sup>2</sup>, Ignacio Payá<sup>3</sup>, Graham J. Pierce<sup>4,5</sup>, Ruben H. Roa-Ureta<sup>6</sup>, Jean-Paul Robin<sup>7</sup>, and Andreas Winter<sup>1</sup>

### ***Cephalopods:***

- Fast population dynamics & weak S-R relationships
- fishery independent survey data rarely comprehensive
- aging expensive & time consuming
- age-based assessment impractical

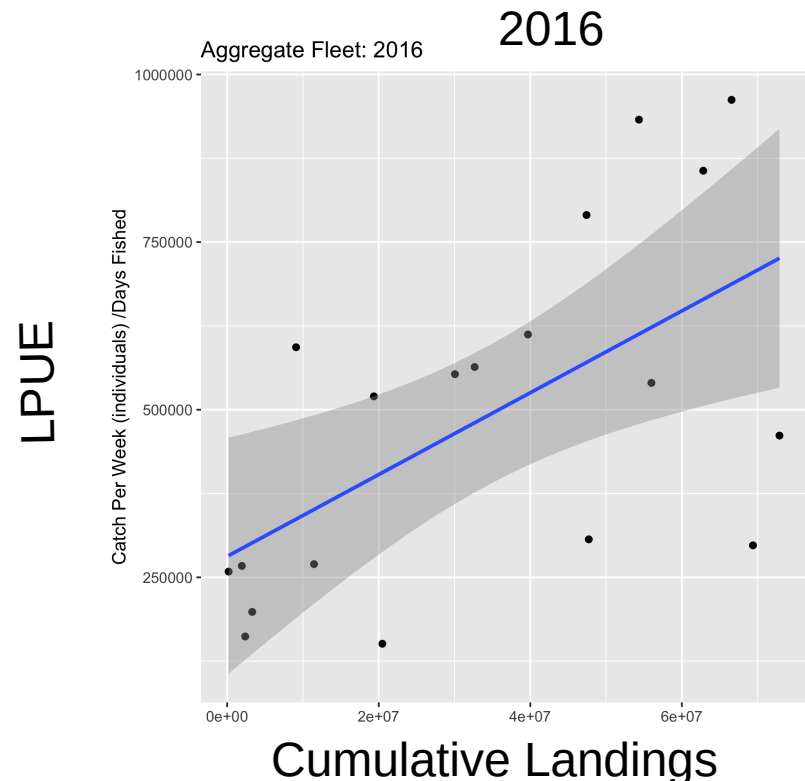
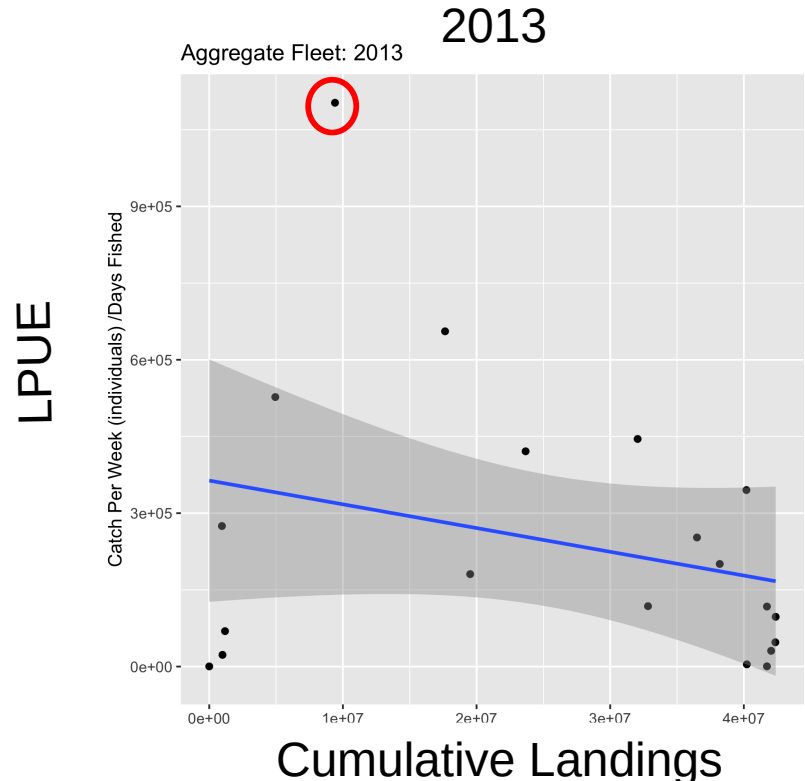
***“Best methods.....”***

***... innovative depletion models fitted with in-season data”***

*Arkhipkin et al. 2020*

# Classical Leslie-Davis modeling applied to Illex fishery

Rago 2020: CPUE decreased continuously in only 4 of 19 years as expected if fishery closed to in-season migration



# Generalized depletion modeling

***Accounts for in-season migration & complex catch-population size relationships***

ICES Journal of  
Marine Science



ICES Journal of Marine Science (2012), 69(8), 1403–1415. doi:10.1093/icesjms/fss110

**Modelling in-season pulses of recruitment and hyperstability-hyperdepletion in the *Loligo gahi* fishery around the Falkland Islands with generalized depletion models**

Rubén H. Roa-Ureta\*

***Requires high frequency records***  
(daily, weekly)

- catch biomass
- effort
- representative individual weights of catch (*to convert catch biomass to number*)

## ***Selected references:***

Roa-Ureta, R.H., 2015. Stock assessment of the Spanish mackerel (*Scomberomorus commerson*) in Saudi waters of the Arabian Gulf with generalized depletion models under data-limited conditions. *Fisheries Research* 171 (2015) 68–77

Lin, Y.-J. et. al. 2017. A stock assessment model for transit stock fisheries with explicit immigration and emigration dynamics: application to upstream waves of glass eels. *Fisheries Research* 195, 130–140.

Maynou, F. et. al 2021 Application of a multi-annual generalized depletion model to the Mediterranean sand eel fishery in Catalonia. *Fisheries Research* 234: 105814

Roa-Ureta, et al 2021, Estimation of the spawning stock and recruitment relationship of *Octopus vulgaris* in Asturias (Bay of Biscay) with generalized depletion models: implications for the applicability of MSY. *ICES Journal of Marine Science*, 78(6) 2256–2270

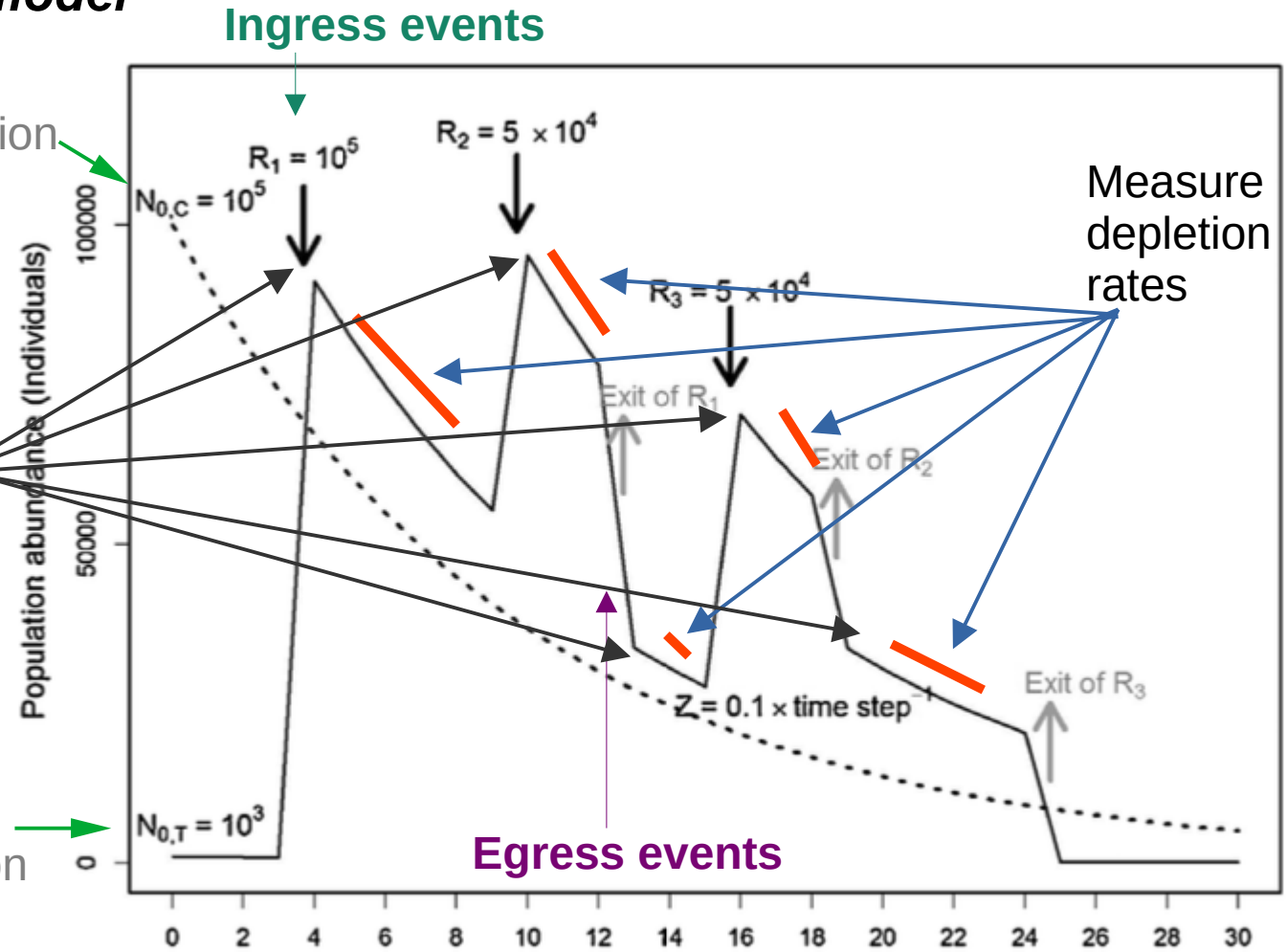
# Generalized depletion modeling: *with open population assumption*

## Conceptual model

Trajectory with closed population  $N_{0,c}$

Restart depletion regression

Trajectory with open population  $N_{0,o}$



# Generalized depletion modeling: Permits nonlinear catchability

$$C_t = kE_t^\alpha N_t^\beta e^{-M/2}$$

$C_t$  = Estimated catch in number at time  $t$

$E_t$  = Fishing effort at time  $t$

$N_t$  = Latent abundance of vulnerable fraction of population at time  $t$

$M$  = natural mortality at time step

$k$  = a scaler (similar to  $q$ )

$\alpha$  = effort response.

$\alpha < 1$  (saturable. gear catches proportionally less with additional effort),

$\alpha \sim 1$  (catch proportional to effort)

$\alpha > 1$  (synergistic. Disproportionate increase in catch with effort increase)

$\beta$  abundance response (fishers perception of true population abundance)

$\beta < 1$  (hyperstability. stable catch when population abundance declines)

$\beta = 1$  (Proportionality. catch tracks population abundance)

$\beta > 1$  (hyperdepletion. catch rate declines faster than population abundance)

Multiple fleets in a fishery can be modeled if  $k, \alpha$ , and/or  $\beta$  sufficiently different

# GDM parameter estimates

- Population:  $N_0$  &  $M \text{ wk}^{-1}$
- Fleet specific:
  - catchability ( $k$ ,  $\alpha$ ,  $\beta$ )
  - Migration events ( $P_{\text{mag}}$ , Timing)

## ***GDM requires:***

- *sound inferences in-season migration timing & magnitude*
- *alot of data (to produce reasonable param/data ratios)*
  - 1 fleet model w/ 1 ingress event = 7 parameters

# Assumptions of classical depletion modeling

*relaxed in GDM*

***1) Population vulnerable to fishery physically & demographically closed***

2) Natural mortality (M) constant

***3) Catch linearly related to population abundance by scaler  $q$***

4) Catchability constant over fishing period & a large pool of animals does not have a refuge &  $q \sim 0$

5) Units of fishing effort are independent & do not compete

6) Fishing capacity is large enough that depletion can be detected & parameters estimated

7) The assumptions of linear regression

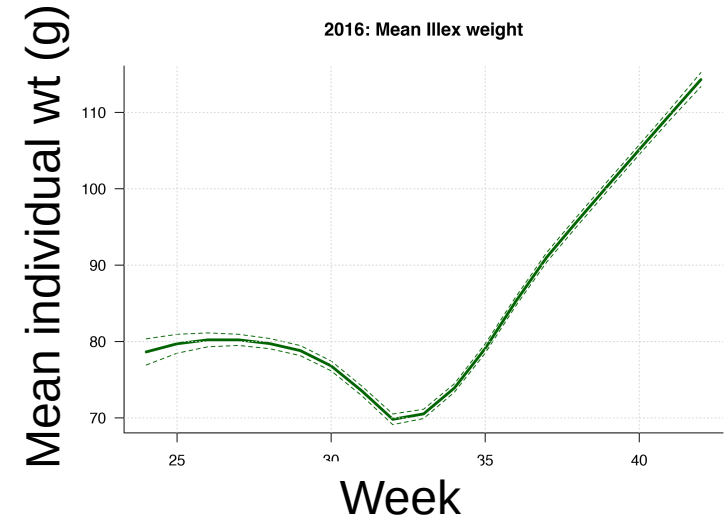
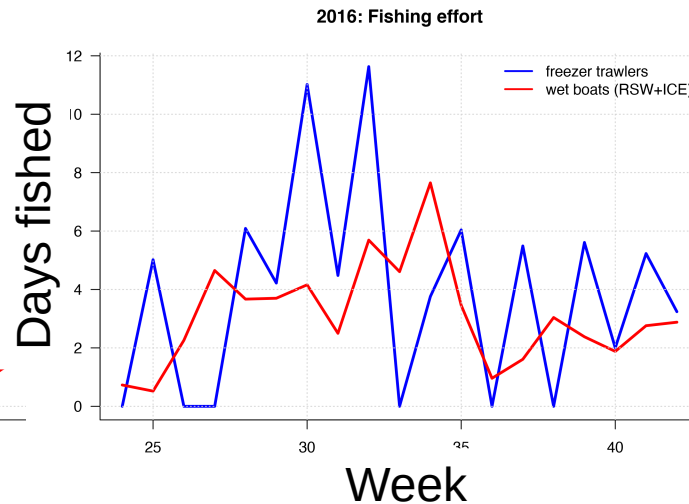
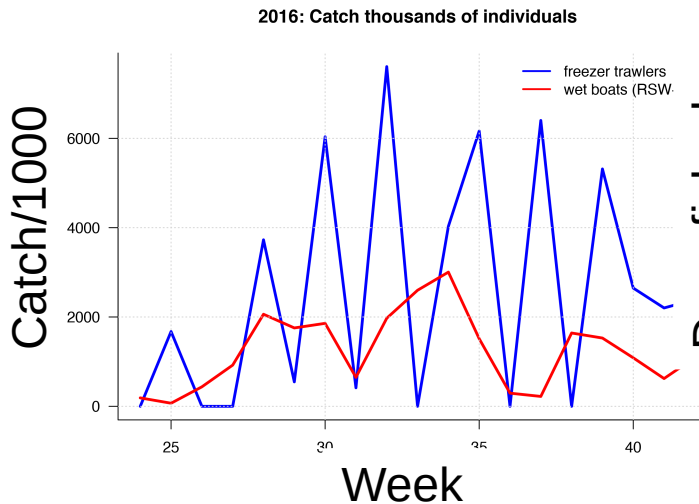


# Generalized depletion modeling: 2016 Illex season

Data: Weekly landings & industry weigh-out data

Year	Date Start	Start Week	End Week	Closure (Wk)	N weeks	Total Catch	% in Data	Fishery condition		#Vessels landing>50k	Days Fished
								Industry	Statistical		
2013	06-10	24	37		14	4,107,000	81	Poor	Poor	12	75
2016	06-13	24	42		19	7,004,000	90	Poor	Poor	10	133
2017	05-02	22	37	37	16	23,371,000	100	Good	Good	20	149
2018	05-28	22	33	33	12	25,524,000	97	Good	Good	26	188
2019	05-02	21	34	34	14	28,495,000	94	Good	Good	32	338

2016 Freezer trawler fleet: 68% of catch & 55% effort



# ***GDM development strategy***

- Step 1: MLE Fit pure depletion GDM w/ closed population assumption.  
Select “best” H0 model variant
- Step 2: Develop hypotheses for open population GDMs.
- Step 3: Fit GDM reflecting open population hypotheses  
& select “best” variants
- Step 4: Select “best” hypothesis from H0....Hn
- Step 5: Use “best” hypothesis model variant to develop parameter estimates & derived quantities

# 2016 Generalized depletion modeling

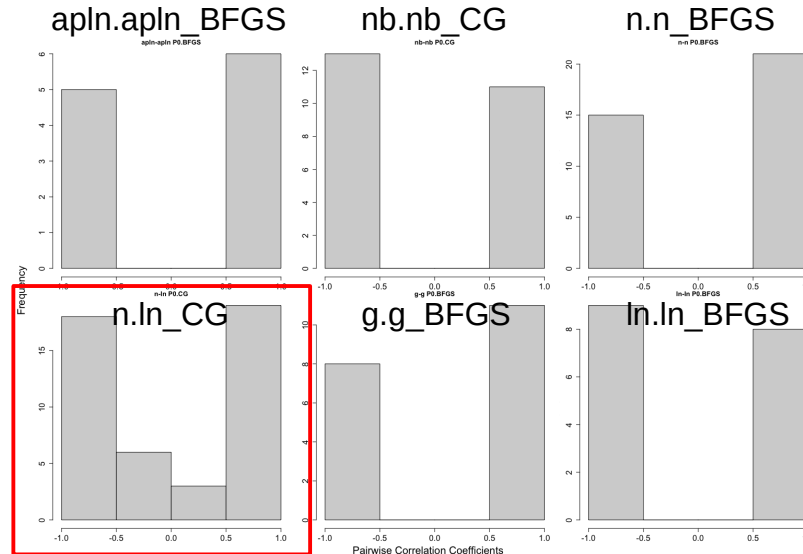
## H0. Pure depletion model w/closed population assumption

Of 48 models specified

7 converged with |param gradients| < 1 & fewer than 2 SE NAs

Distribution	Method	Max.Abs.Grads.	M	M_%CV	N0	N0_%CV	SE_Nas
aplnormal,aplnormal	BFGS	0.08	0.00001	4148.4156	289,232,685	46	0
negbin,negbin	CG	0.02	0.00015	2153.72601	29,821,419	2225	0
normal,normal	BFGS	0.07	0.00000	8958.41323	6,929,326,679	NA	1
lognormal,normal	CG	0.20	0.00138	438.812067	4,179,970	57	2
normal,lognormal	CG	0.15	0.00033	461.892935	17,968,406	90	2
lognormal,lognormal	BFGS	0.14	0.00003	1978.01903	180,676,740	2027	2
gamma,gamma	BFGS	0.05	0.00004	4559.80348	520,690,210	NA	2

Parameter  
Correlations



**Biological realism**

- M low by orders of magnitude
- suggests squid ingress

# ***GDM development strategy***

Step 1: Fit a pure depletion GDM ( $H_0$ ) with closed population assumption.

Select “best” model variant

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Step 5: Use “best” hypothesis model variant to develop parameter estimates and derived quantities

# Catch perturbation analysis

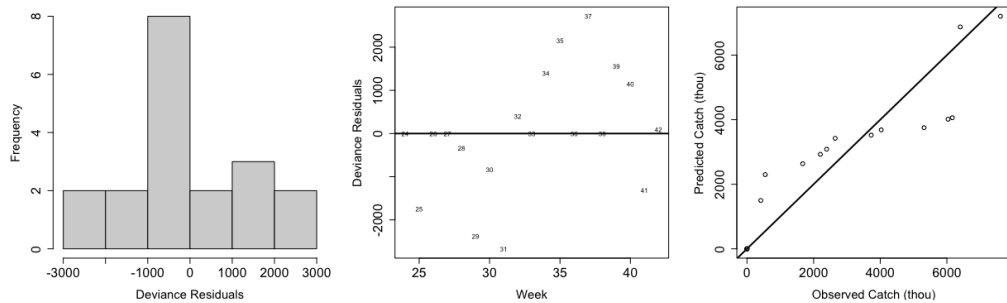
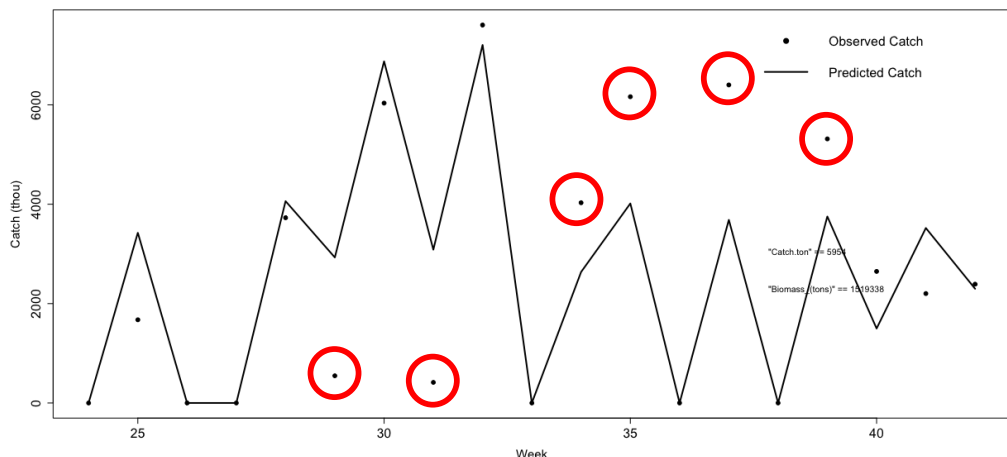
2016: Residuals of (H0) pure depletion model

illill.2016\_F2P0.0.n.In.fit.pred.CG

Used primarily for open population hypothesis development

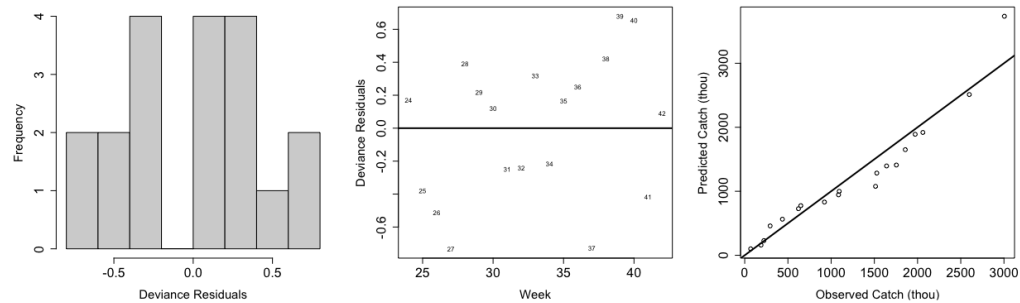
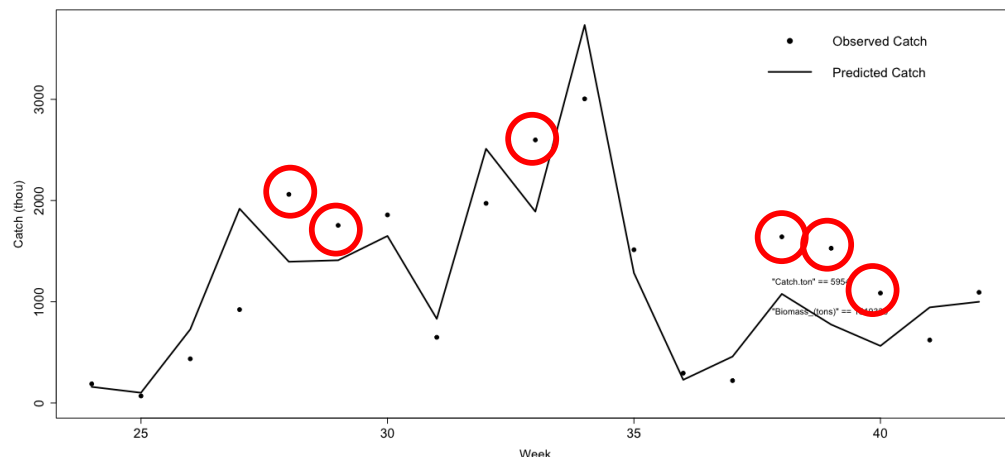
## Freezer trawlers

Fleet = freezer, Perturbations = 0, Distribution = Normal, Numerical algorithm = CG



## Wet boats (RSW + ICE)

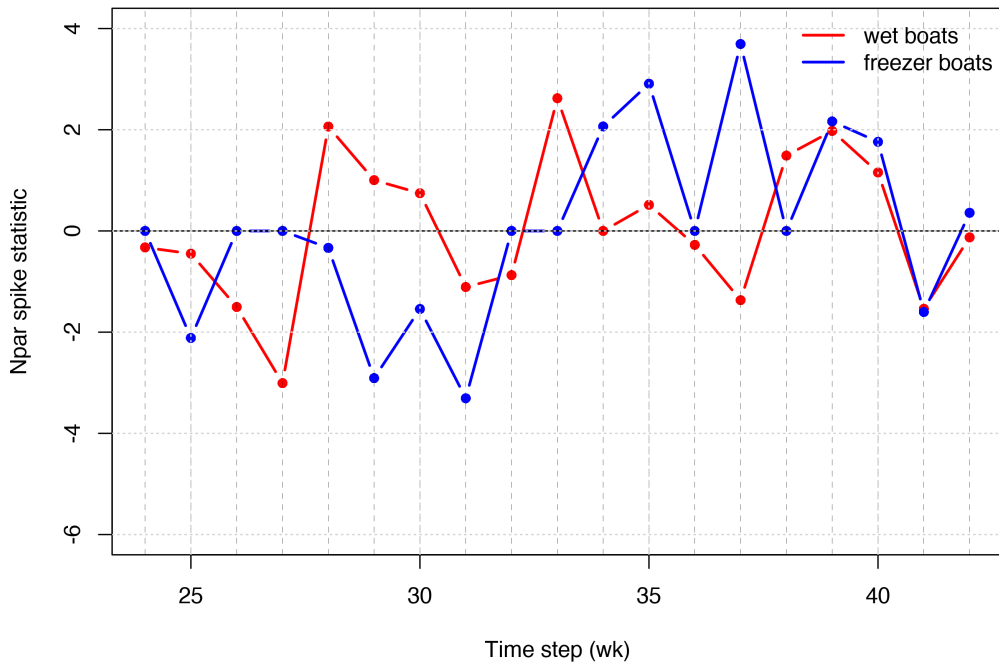
Fleet = wet, Perturbations = 0, Distribution = Lognormal, Numerical algorithm = CG



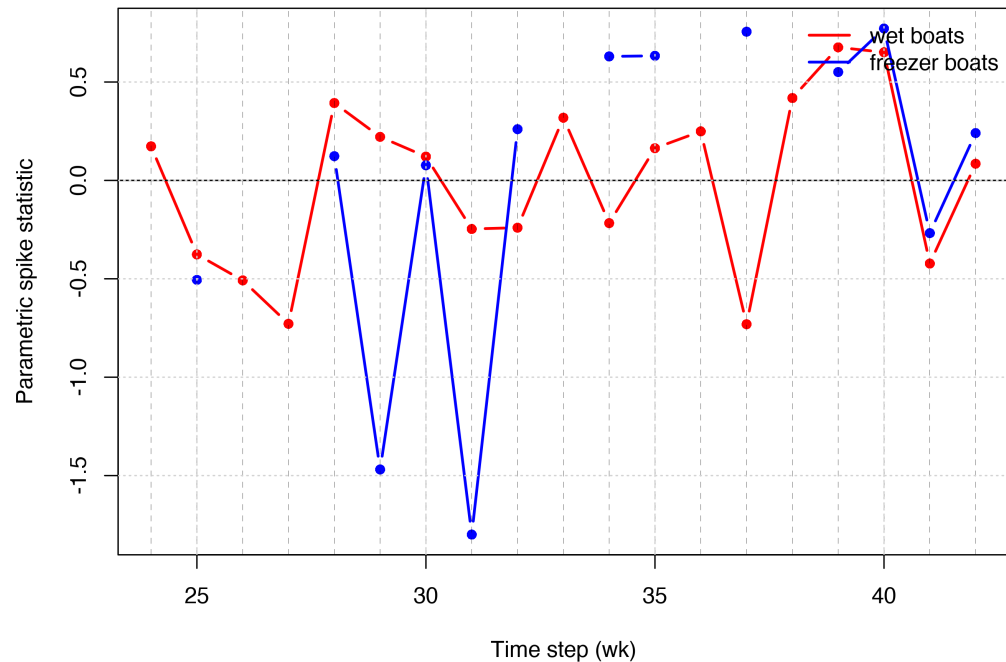
# Catch perturbation analysis

2016: Catch spike statistics. Anomalies in catch standardized by effort

2016 : Nonparametric catch spike statistic



2016 : Parametric catch spike statistic

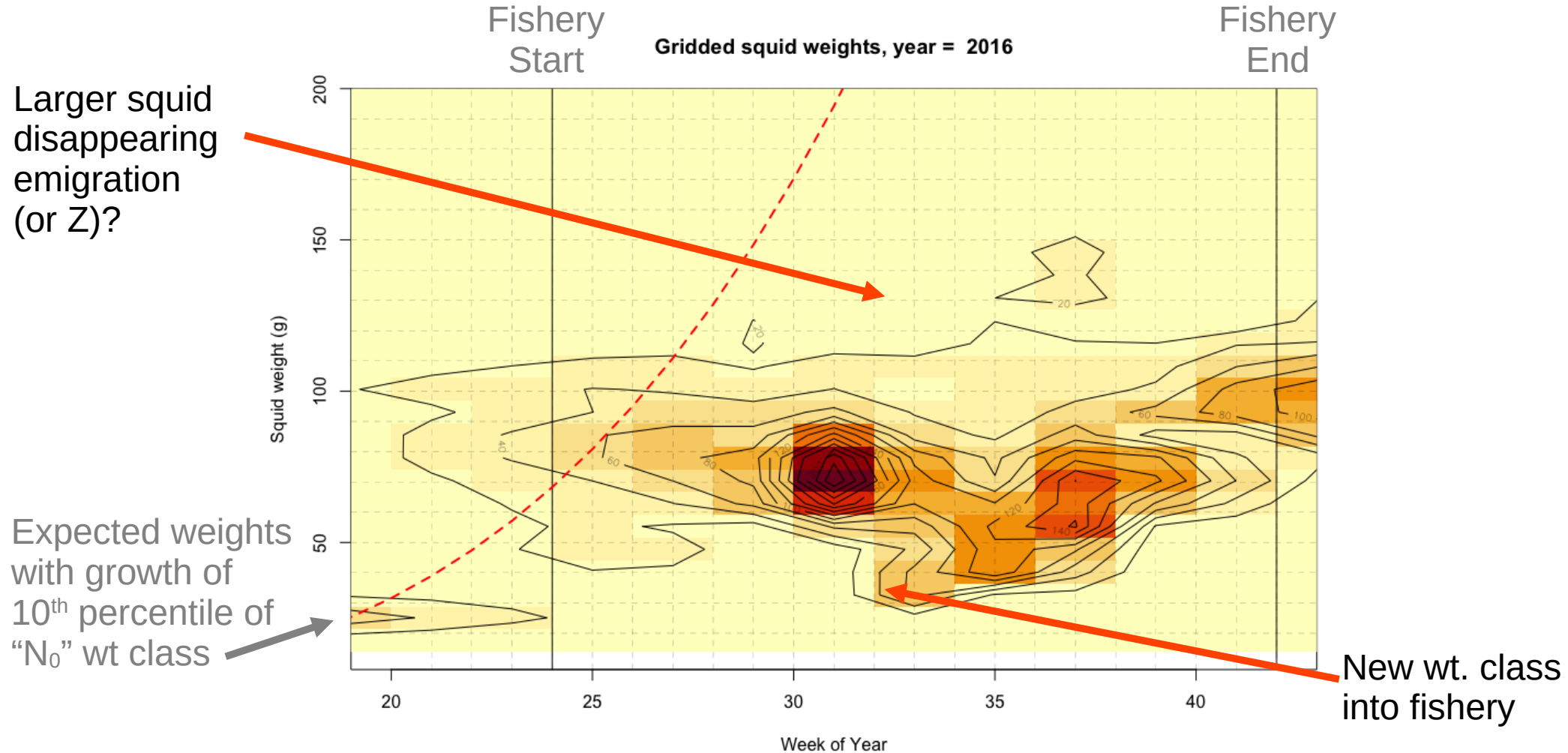


Freezer week: 25-, 29-, 31-, 35+, 37+, 39+  
Wet week: 25-, 27-, 29+, 33+, 37-, 39+

Freezer week: 29-, 31-, 34+, 35+, 37+, 39+, 40+  
Wet week: 27-, 28+, 33+, 37-, 38+, 39+

# Catch perturbation analysis

2016: Weight frequencies from industry data



# Catch perturbation analysis

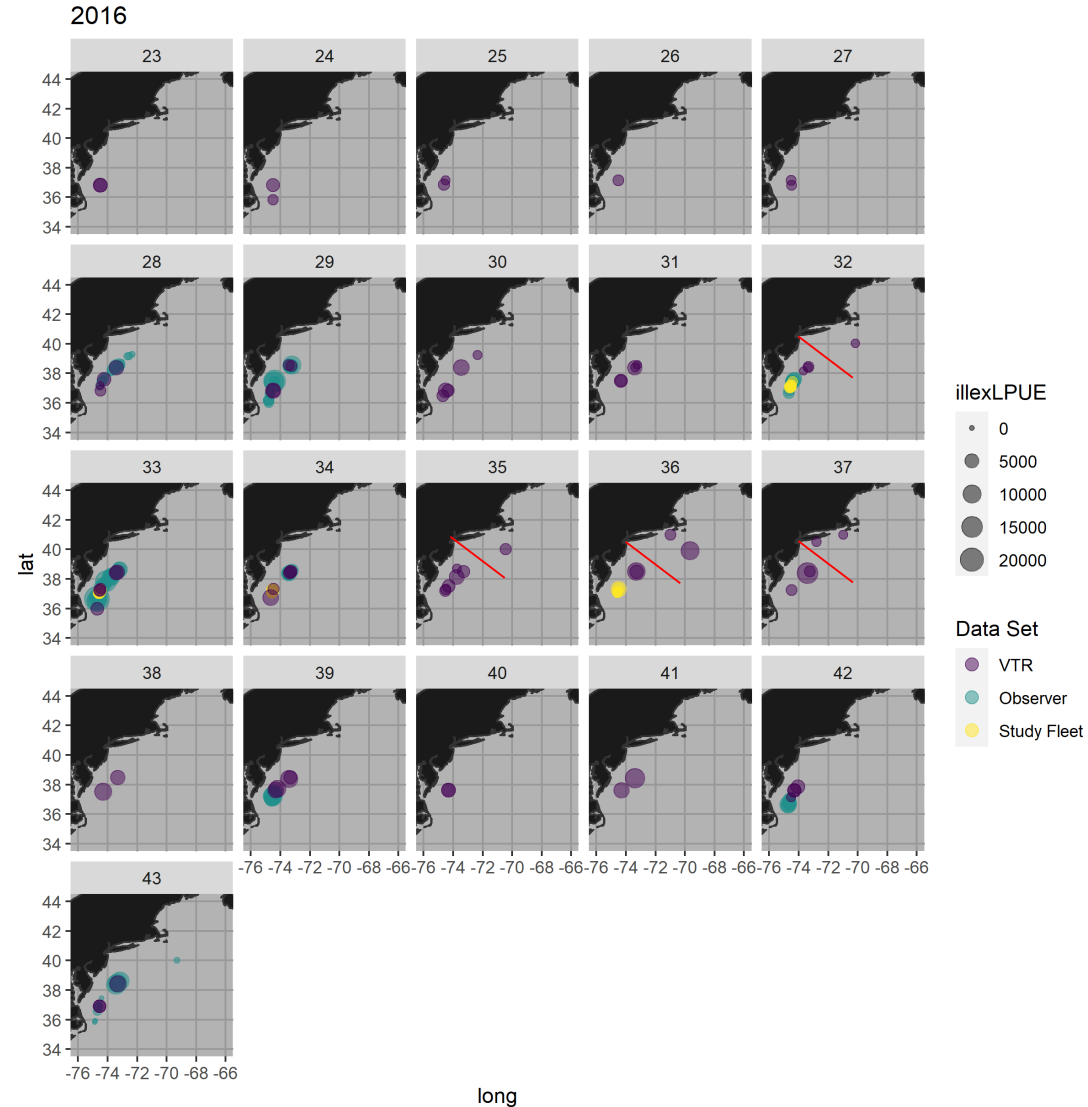
## 2016: Fleet dynamics

### Catch relative to Hudson Self Valley

Persistent catch SW all weeks

Weeks 23-31, 33-34, 38-43

Some catch NE weeks 32, 35-37





# Catch perturbation analysis

2016: Perturbation summary table

Week	Fleet Dyn	Wt. Freq	Freezer				Wet				Hypothesis	Timings Wk
			DF	H0_resid	N Par	Par	DF	H0_resid	N Par	Par		
24	SW		0				0.73					
25	SW		5.02		-		0.52					
26	SW		0				2.26				E1.wet= -27	
27	SW		0				4.65	-	-		E1.freeze= -29	
28	SW		6.09				3.67	+	+	+	H3: P1E1P2E1 P1.wet=33	
29	SW		4.22	-	-	-	3.7				P1.freeze=34	
30	SW	+	11.02				4.16				P2.wet=38	
31	SW		4.48	-	-	-	2.5					
32	SW & NE	+	11.63				5.69					
33	SW		0				4.61	+	+		H1: P1P1 P1.wet=33	
34	SW	+	3.76	+		+	7.65	-			P1.freeze=34	
35	SW & NE	+	6.04	+	+	+	3.46					
36	SW & NE		0				0.96					
37	SW & NE		5.49	+	+	+	1.61	+		-		
38	SW		0				3.04	+		+		
39	SW		5.61		+	+	2.38	+	+	+	H2: P2P2 P1.wet=33	
40	SW		2			+	1.88	+		+	P1.freeze=34	
41	SW		5.23				2.76				P2.freeze=37	
42	SW		3.24				2.88				P2.wet=38	
Total			73.8				59.1					
# Effort			56				44					

# ***GDM development strategy***

- Step 1: Fit a pure depletion GDM ( $H_0$ ) with closed population assumption.  
Select “best” model variant
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- Step 5: Use “best” hypothesis model variant to develop parameter estimates and derived quantities

# 2016 Generalized depletion modeling

Parameter estimates of “best” model variants for H1 & H2a,b. (H3 variants fail criteria)

Produced SEs  
Most CV < 100  
M Reasonable  
Parsimonious

**H0:**

Best H0 variant 2016. P0P0 normal, alognormal_CG						
Parameter	Timing.freezer	Estimates.freezer	CVpCent.freezer	Timing.wet	Estimates.wet	CVpCent.wet
M.1/week		0.0003	462		0.0003	462
N0.thou		17,968,406	90		17,968,406	90
k.1/Days Fished		0.0001	NA		0.0001	5714
alpha		1	25		1	11
beta		0.95044	NA		0.91990	371
psi.thou.squared		1910874.32	33		0.18	33

**H1:**

P1.freezer ← +34  
P1.wet ← +33

Best H1 variant 2016. P1P1 aplognormal, aplognormal_BFGS						
Parameter	Timing.freezer	Estimates.freezer	CVpCent.freezer	Timing.wet	Estimates.wet	CVpCent.wet
M.1/week		0.026	57		0.026	57
N0.thou		26,221,404	7		26,221,404	7
Rec.thou.Wave1	08-28_09-03	90,828	5657	08-14_08-20	37,092,712	22
k.1/Days Fished		0	8		2	168
alpha		1.61655	3		1.33916	11
beta		1.67	1		0.29	33

**H2:**

P1.freezer ← +34  
P1.wet ← +33  
P2.freezer ← +37  
P3.wet ← +38

Best H2 variant 2016. P2P2 normal,normal_CG						
Parameter	Timing.freezer	Estimates.freezer	CVpCent.freezer	Timing.wet	Estimates.wet	CVpCent.wet
M.1/week		0.006	309		0.006	309
N0.thou		448,208	185		448,208	185
Rec.thou.Wave1	08-14_08-20	149,517	NA	08-14_08-20	39,457	NA
Rec.thou.Wave2	09-11_09-17	34,734	1025	09-11_09-17	18,546	1887
k.1/Days Fished		0.00003	416		0.00016	858
alpha		0.81	25		0.91	20
beta		1.31	27		1.13	25
psi.thou.squared		1131468	37		191868.52	35

Most CV < 100  
M Reasonable  
Missing SEs  
Less Parsimony

**H2b:**

P1.freezer ← +34  
P1.wet ← +33  
P3.wet ← +38

Best 2016 H2b variant. P1P2 normal, lognormal_CG.						
Parameter	Timing.freezer	Estimates.freezer	CVpCent.freezer	Timing.wet	Estimates.wet	CVpCent.wet
M.1/week		0.013	246		0.013	246
N0.thou		74,581	84		74,581	84
Rec.thou.Wave1	08-28_09-03	56,559	74	08-28_09-03	21,964	84
Rec.thou.Wave2				08-14_08-20	16,036	91
k.1/Days Fished		0.00002	168		0.00036	NA
alpha		1.28	14		1.42	12
beta		1.51	16		1.19	NA
psi.thou.squared		502500	41		0.23	21

# 2016 Generalized depletion modeling

“Best” hypothesis (P1P1) & model variant (apln.apln.BFGS)

## Choice based upon

- numerical, statistical, biological realism criteria
- confirmed using AIC & variants with same distribution assumptions

Best H1 variant 2016. P1P1 aplognormal, aplognormal\_BFGS

Parameter	Timing.freezer	Estimates.freezer	CVpCent.freezer	Timing.wet	Estimates.wet	CVpCent.wet
M.1/week		0.026	57		0.026	57
N0.thou		26,221,404	7		26,221,404	7
Rec.thou.Wave1	08-28_09-03	90,828	5657	08-14_08-20	37,092,712	22
k.1/Days Fished		0	8		2	168
alpha		1.61655	3		1.33916	11
beta		1.67	1		0.29	33

% CV > 100

# 2016 Generalized depletion modeling

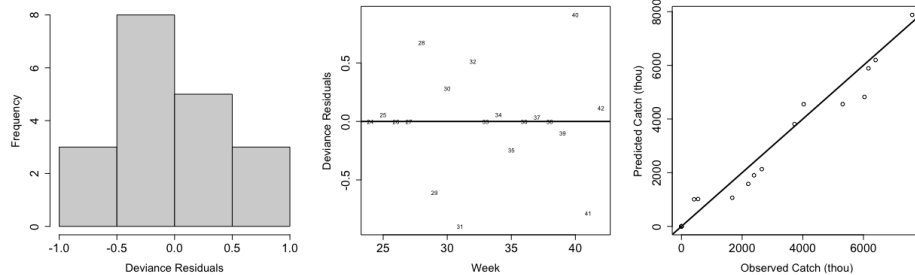
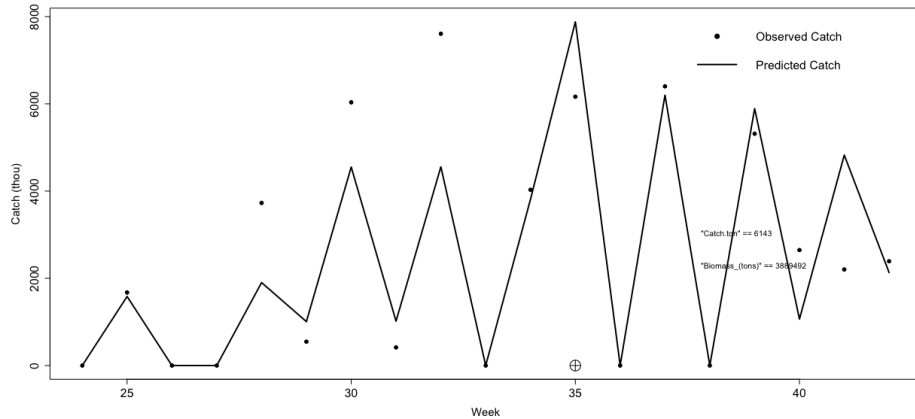
Model fit for "best" H1 model variant

illll.2016\_F2P1E0P1E0.0.apln.apln.pred.BFGS

In-season pulses : 08-28\_09-03

Freezer trawlers

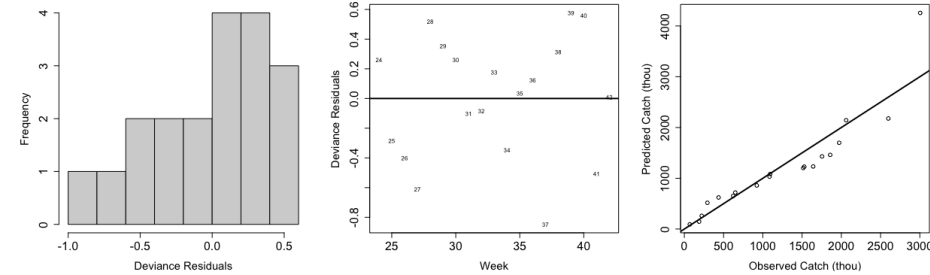
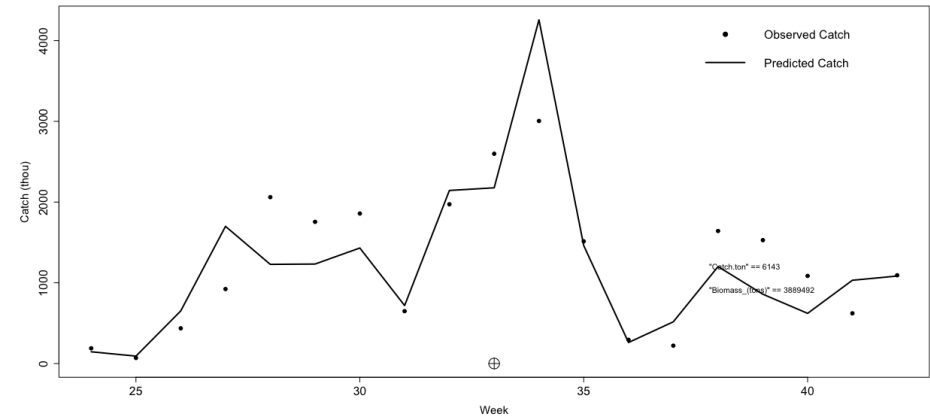
Fleet = freezer, Perturbations = 1, Distribution = Aplnormal, Numerical algorithm = BFGS



08-14\_08-20

Wet boats (RSW + ICE)

Fleet = wet, Perturbations = 1, Distribution = Aplnormal, Numerical algorithm = BFGS



# ***GDM development strategy***

Step 1: Fit a pure depletion GDM ( $H_0$ ) with closed population assumption. Select “best” model variant

Step 2: Develop hypotheses for open population GDMs.

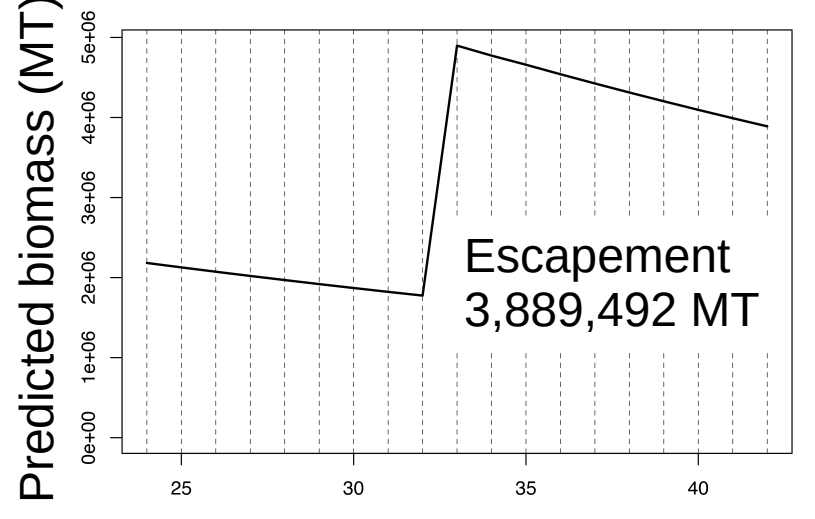
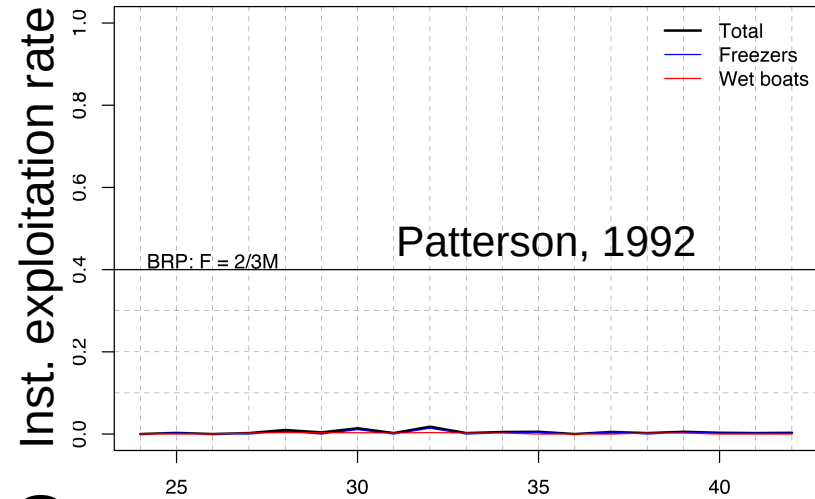
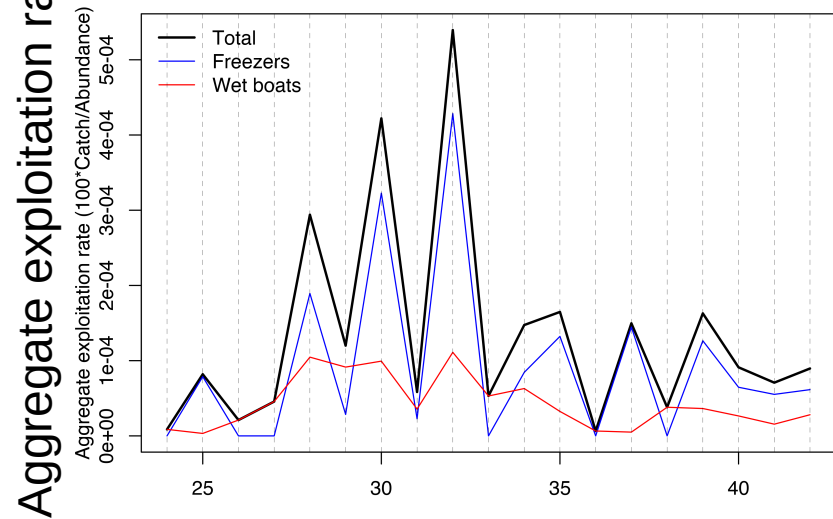
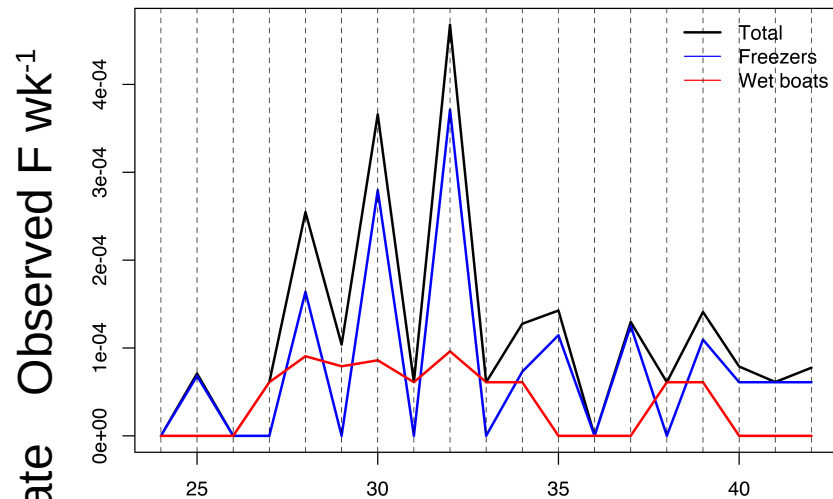
Step 3: Fit GDM reflecting open population hypotheses & select “best” variants

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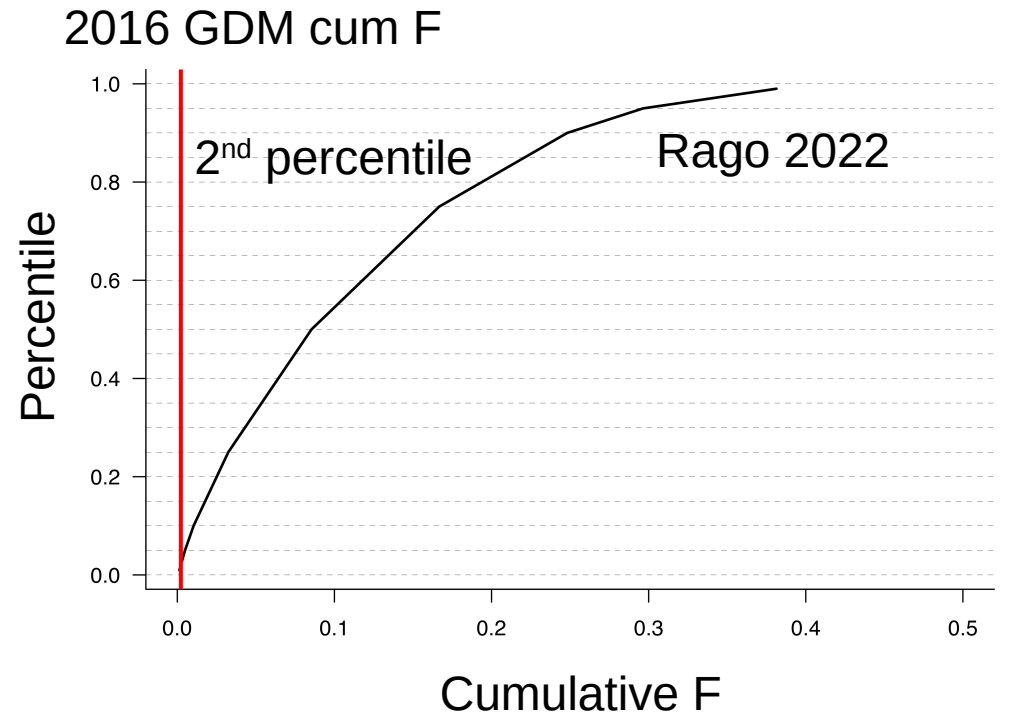
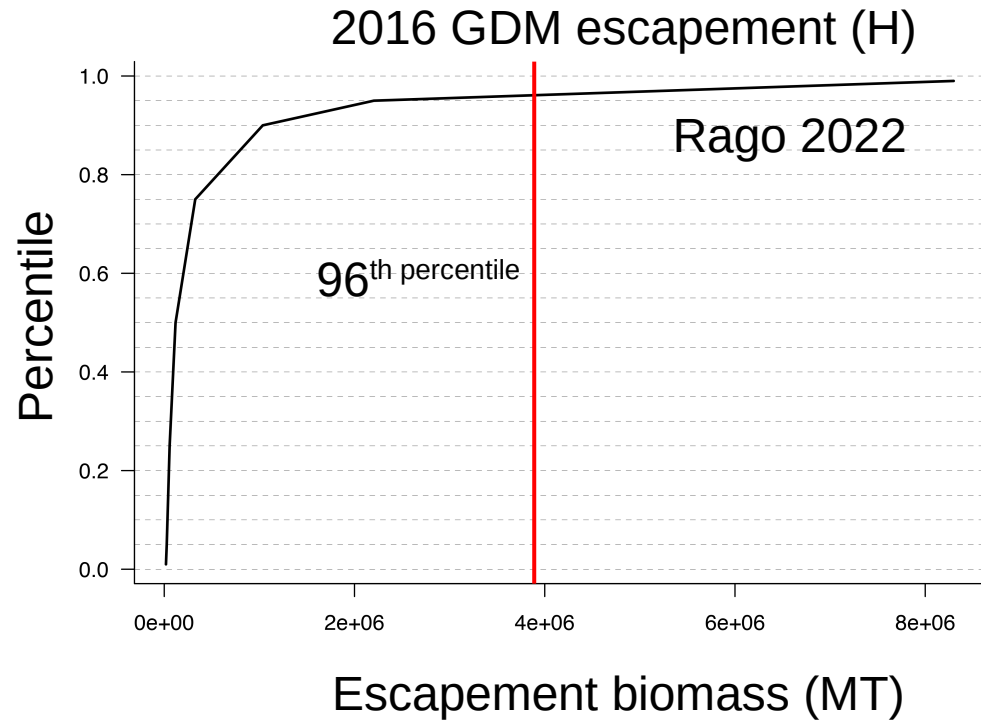
# 2016 Generalized depletion modeling

Derived quantities of interest: *illill.2016\_F2P1E0P1E0.0.apln.apln.pred.BFGS*



# 2016 GDM vs Rago 2022 plausible bounds

Comparison of GDM fishery based estimates  
(*illill.2016\_F2P1E0P1E0.0.apln.apln.pred.BFGS*)  
with Rago 2022 FI survey based estimates





# Generalized depletion modeling 2013-2019

“Best” hypotheses & variants. Important issues related to sample size

## Catch-ability parameters

Season	Model	Distribution	Method	k.freezer	%_CV	alpha.fr	%_CV	beta.fr	%_CV
2013	0P1P	Negbin	BFGS	4.97E+02	110	1.12	44	0.01	1504
2016	1P1P	Apln	BFGS	5.63E-11	8	1.62	7	1.67	1
2017	1P1P	Normal	BFGS	4.70E-06		0.84	15	1.10	
2018	0P0P	Gamma	BFGS	4.83E-05	4524	0.44	33	1.11	126
2019	1P2P	Normal	BFGS	8.30E-02		0.46	9	0.54	31

 % CV (SE/Est\*100) > %100 or asymptotic SE not produced

Season	Model	Distribution	Method	k.wet	%_CV	alpha.wet	%_CV	beta.wet	%_CV
2013	0P1P	Negbin	BFGS	2.25E-11		0.47	51	2.49	
2016	1P1P	Apln	BFGS	1.52E+00	2	1.34	11	0.29	33
2017	1P1P	Normal	BFGS	4.26E-02	4	0.72	14	0.59	32
2018	0P0P	Gamma	BFGS	1.67E-04	51	1.17	63	0.93	256
2019	1P2P	Normal	BFGS	1.07E-02		0.53	28	0.65	

## Catch perturbations (in-season immigration)

Season	Model	P1.Mag.fr.thou	%_CV	Wk.P1.fr
2013	0P1P			
2016	1P1P	90,828	5657	35
2017	1P1P	17,354	3718	24
2018	0P0P			
2019	1P2P	4,361	10363	27

## Fleet specific parameters

Catch-ability & catch perturbations

### 2019 1P2P model

N weeks = 14

2 ingress events into wet boat fleet

3 catchability params,

2 perturbations (\*2 params) = 4

= 7 params

param/data= 7/14 = 0.5

Season	Model	P1.Mag.wet.thou	%_CV	Wk.P1.wet	P2.Mag.wet.thou	%_CV	Wk.P2.wet
2013	0P1P	287,091	443				
2016	1P1P	37,092,712	22	33			
2017	1P1P	63,596,193	NA	23			
2018	0P0P						
2019	1P2P	66,271,954	684	26	62,144,970	731	31

# ***Generalized depletion modeling 2013-2019***

## ***Sample sizes***

***- With weekly time step insufficient***

Season	Weeks	Model	N Params	Weekly step		Daily step	
				N_data_wk	Param/Data	N_data_day	Param/Data
2013	14	0P1P	10	28	0.36	98	0.10
2016	19	1P1P	12	38	0.32	133	0.09
2017	16	1P1P	12	32	0.38	133	0.11
2018	12	0P0P	8	24	0.33	84	0.10
2019	14	1P2P	14	28	0.50	98	0.14

## ***Daily time step***

***- increase precision***

***- Increase ability to detect in-season migration events including emigration***

***\*Pulses have large influence on quantities of interest***

***- Probably need catch rather than landings (0 inflation problem for freezer trawlers)***

# ***Generalized depletion modeling***

- Could allow risk of overfishing to be assessed while accounting for in-season migration
- Could allow for in-season assessment
- Weekly landings data insufficient & existing weight data not fully representative

## ***Next steps***

### ***1) Near term.***

Combine data simulation with analysis of existing landings and shorter time step.

a) Can existing landings data with shorter step provide sufficient precision & sensitivity to ingress/egress events? (probably not)

b) Data simulation

Evaluate impacts of sample size, data quality, ingress/egress on parameter sensitivities

c) Develop methods to generate full suite of uncertainty estimates for quantities of interest

### ***2) Medium term***

Based on findings of #1) develop collaborative research study/experimental fishery to...

a) develop in-season data & information streams to support GDM

Include in-season information sharing between fishery, assessors and fisheries oceanographers to get inferences about migration right

b) pilot study: evaluate utility of approach in operational assessment